

n	0	1	2	3	4	5	6	7	8	9	10	1
p	1	8	4	28	172	989	518	2201	4804	1662	245	3
		8	8	8	6	08	11	67	76	7	2	

$$\sigma = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 2 & 1 \end{pmatrix} = (1 \ 3 \ 5)(2 \ 4) = (1 \ 5)(1 \ 3)(2 \ 4).$$

So, there are many other ways of obtaining a composition of transpositions

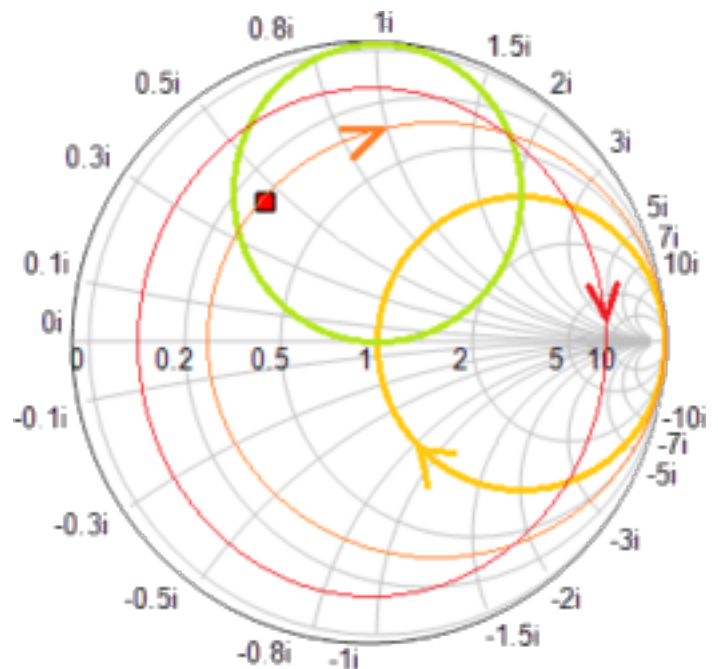
A function  $g(n)$  is an asymptotic approximation to  $f(n)$  if  $f(n)/g(n) \rightarrow 1$  as  $n \rightarrow \infty$

$$F(x) = \sum_{n=0}^{\infty} \frac{f_n}{n!} x^n$$

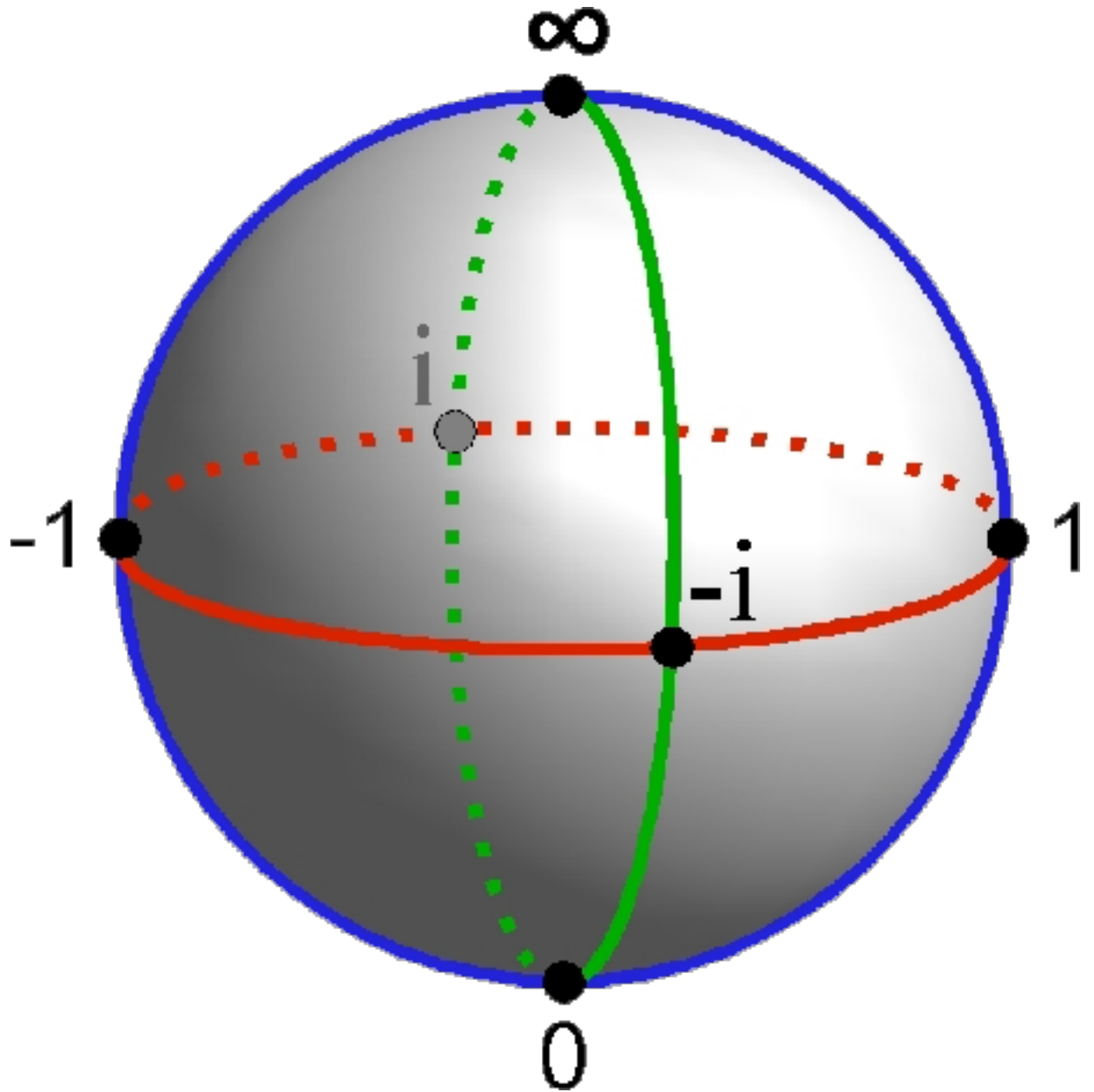
$$1 + F'(x) - [F'(x)]^2 + [F'(x)]^3 + \dots = \frac{1}{1 - F(x)}$$

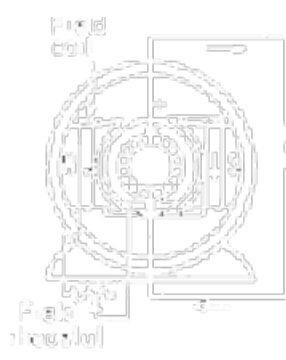
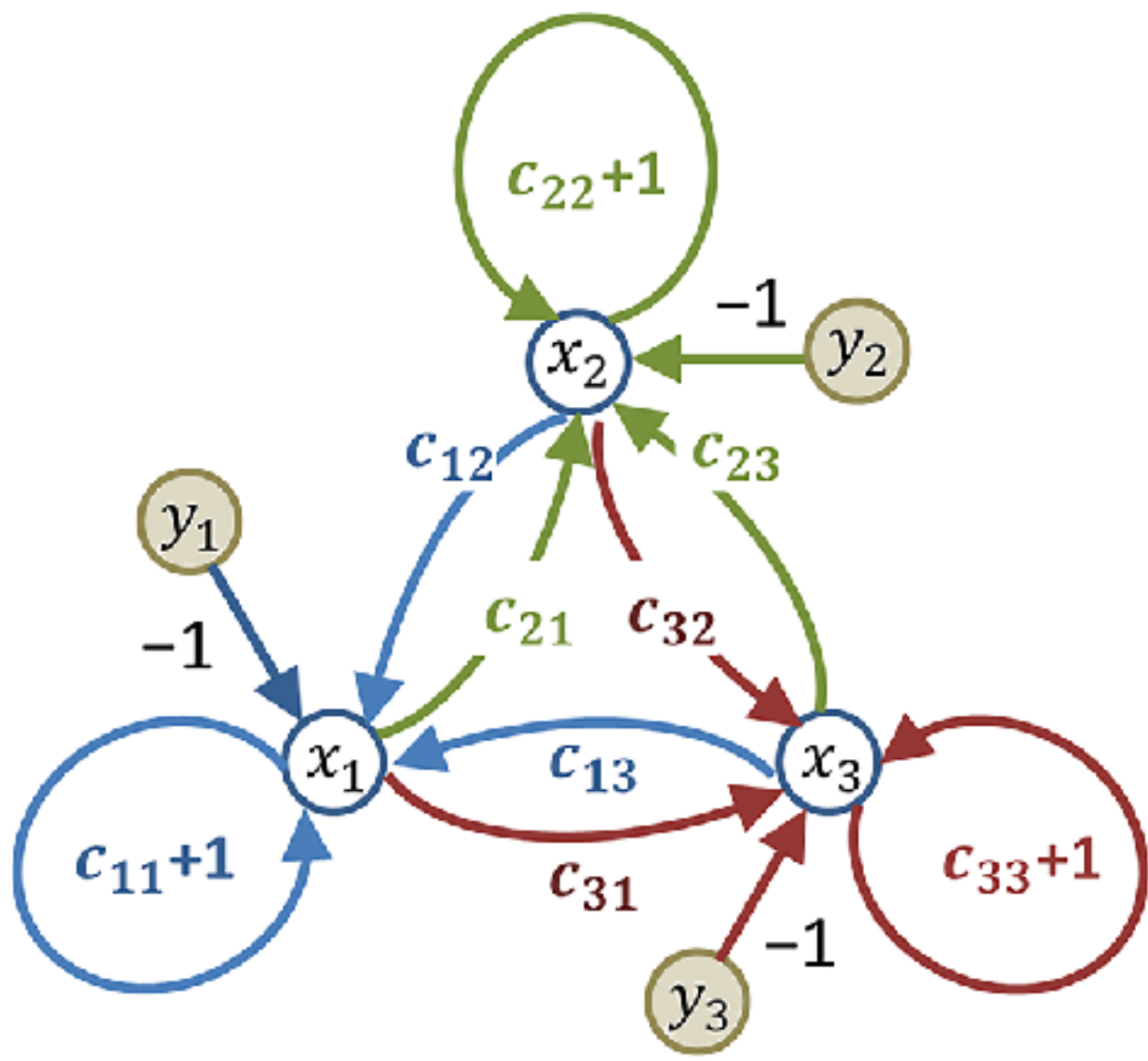
$$P(x) = \frac{1 - \sqrt{1 - 4x}}{2}$$

$$\mathcal{P} = \{\bullet\} \times \text{Seq}(\mathcal{P})$$

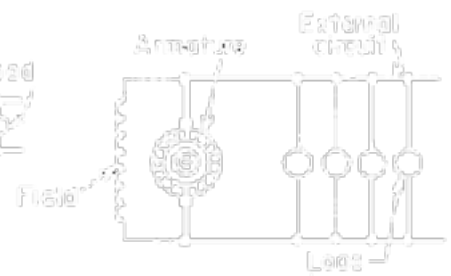


n	f	p
0	1	1
1	9	6
2	54	27
3	32	12
	1	0
4	18	53
	47	4
5	99	22
	92	56

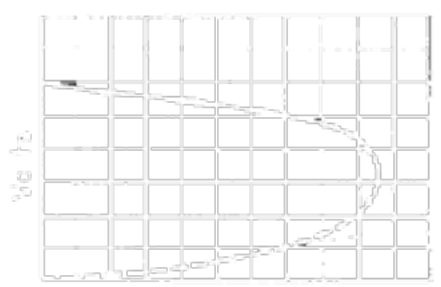




I- Diagram



II- Elementary circuit



III- Energetic graph

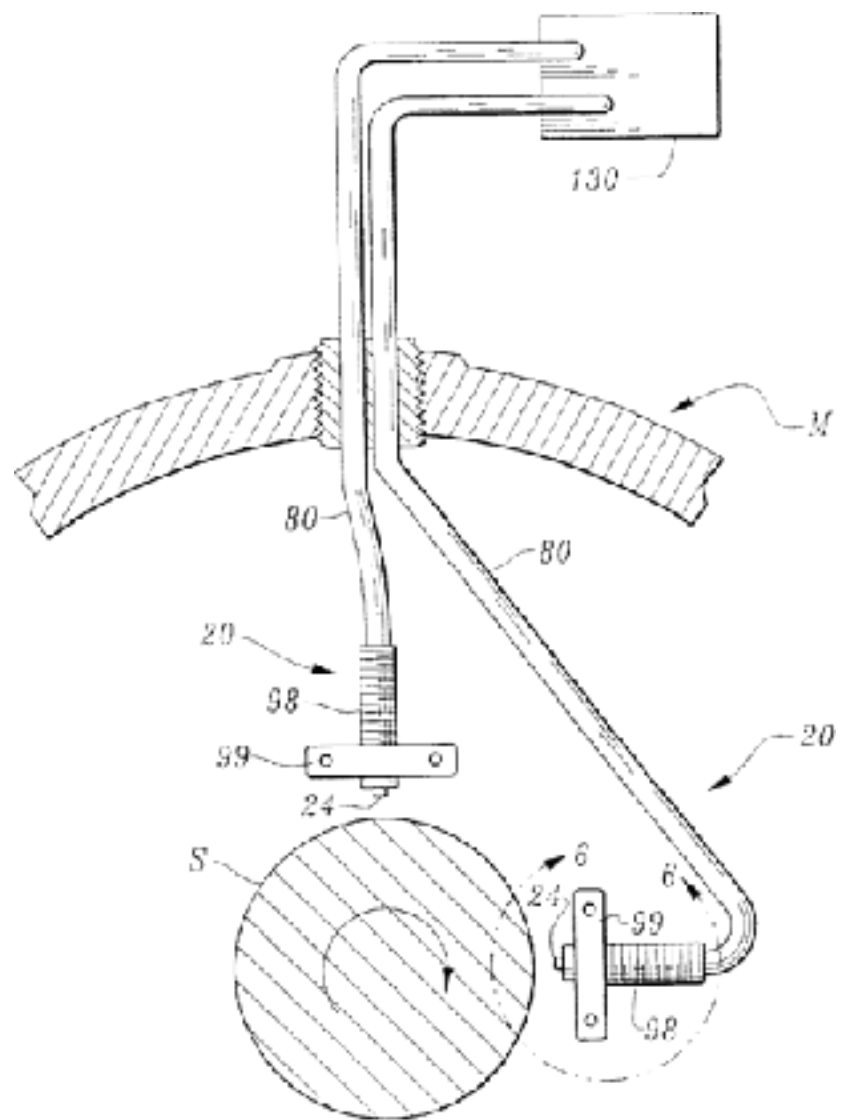
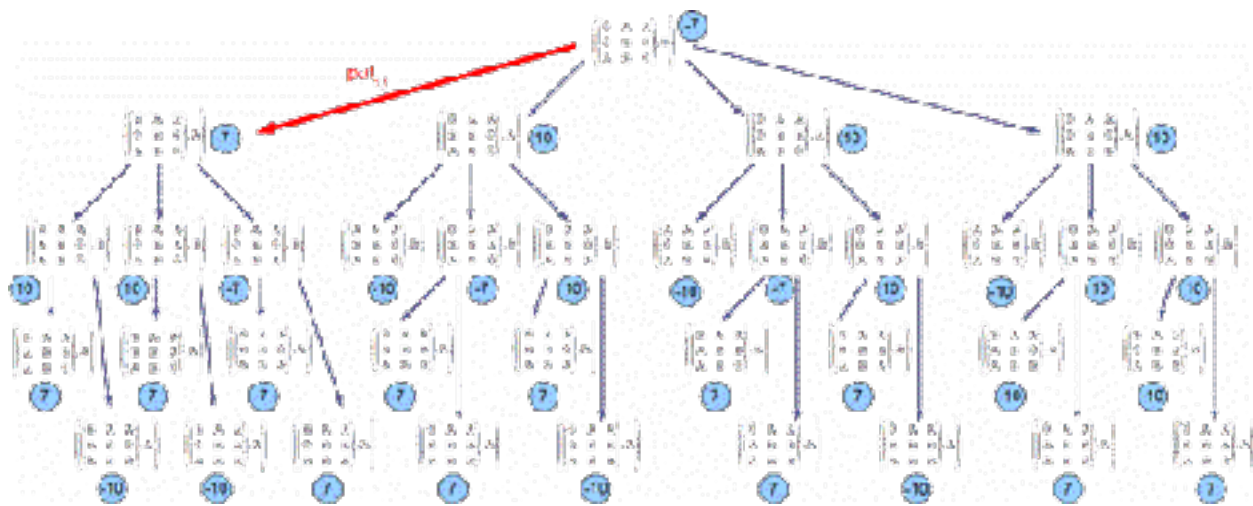
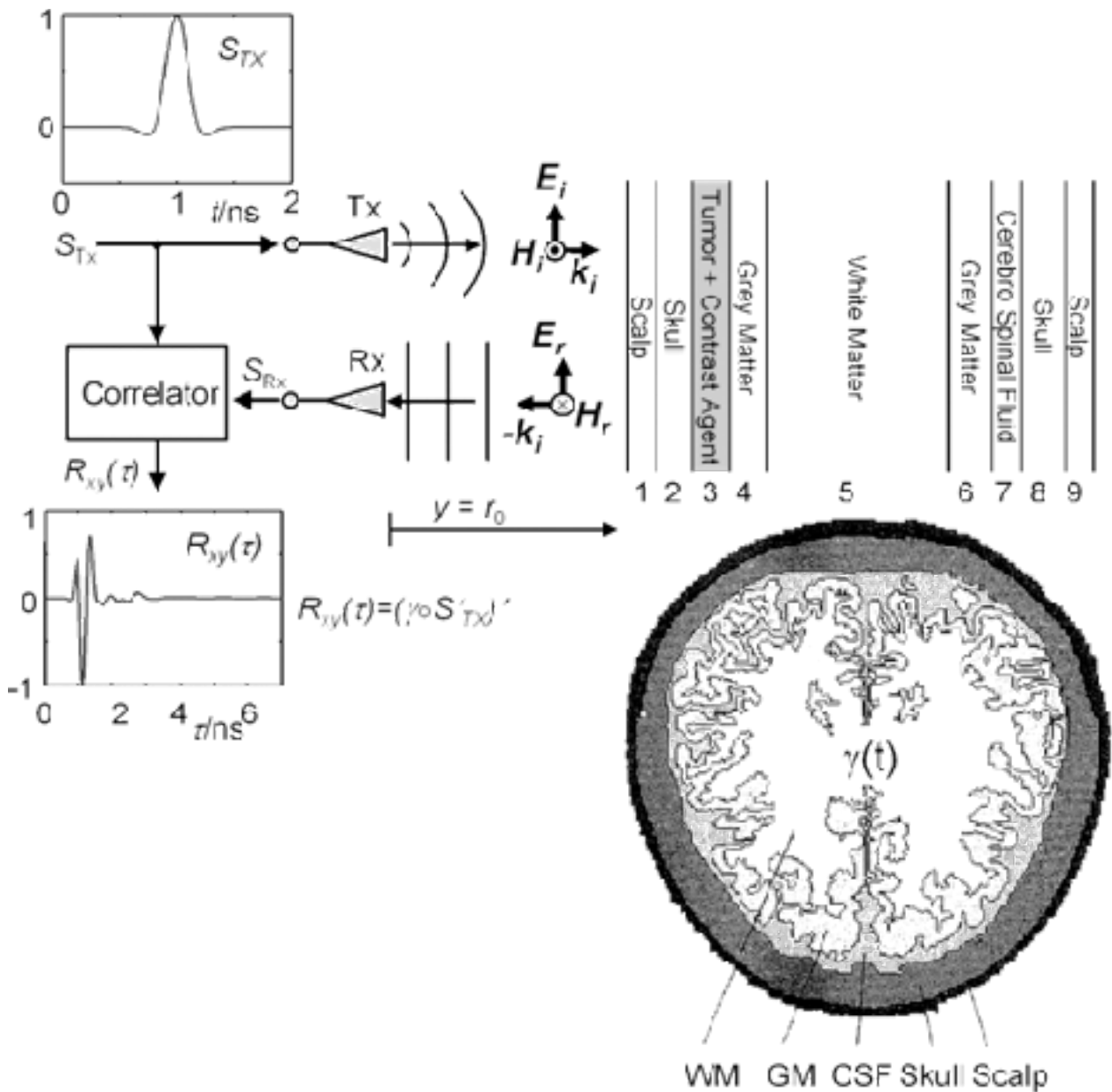
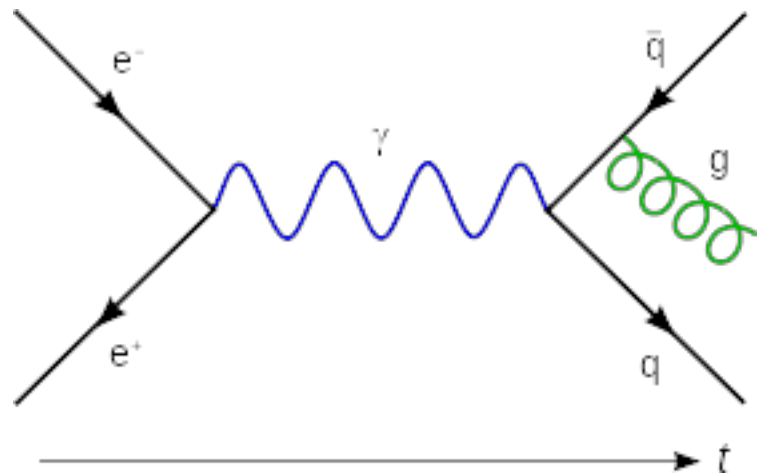
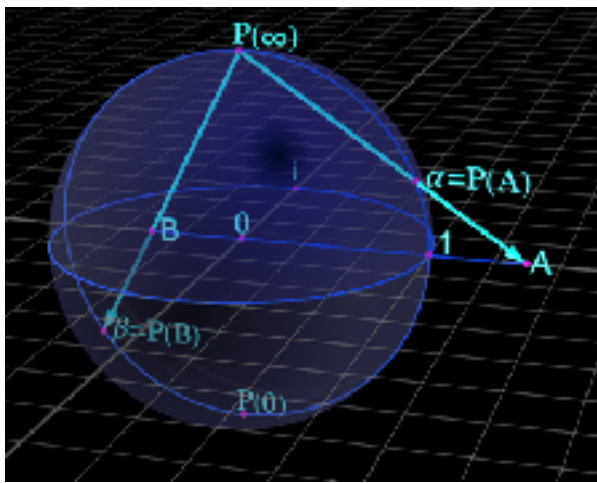
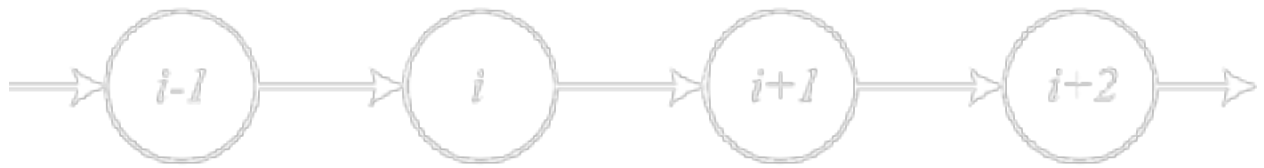


Fig. 5



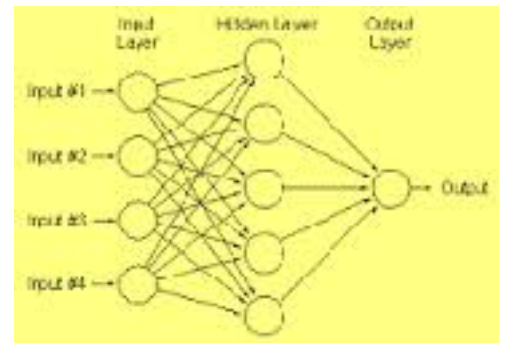
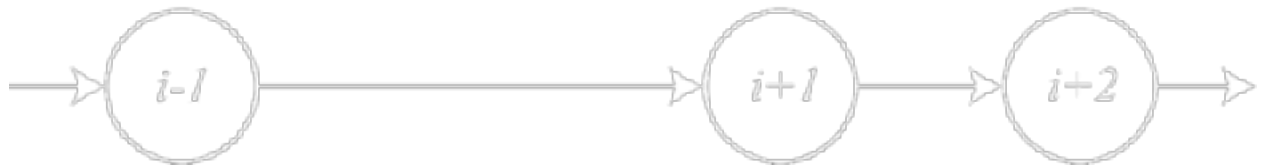
### Initial State of the Linked List



### Linked List After the Removal Operations



### Resultant Linked List



Given two statistical possibilities,  $\mathcal{F}$  and  $\mathcal{G}$ , with generating functions  $F(x)$  and  $G(x)$  respectively, the *disjoint union of the two possibilities* ( $\mathcal{F} \cup \mathcal{G}$ ) has generating function  $F(x) + G(x)$ .

$$C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!} = \prod_{k=2}^n \frac{n+k}{k} \quad \text{for } n \geq 0.$$

The first Catalan numbers for  $n = 0, 1, 2, 3, \dots$  are

1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58.786K, 208.012K, 742.900K

As 'C', the Catalan numbers have an integral representation

$$C_n = \int_0^1 x^n p(x) dx$$

Asymptotically, the Catalan numbers grow as

$$C_n \sim \frac{4^n}{n^{3/2} \sqrt{\pi}}$$

Note that

$$\ln(n!) = n \ln(n) - n + O(\ln(n))$$

Where  $O$  represents *Observations*

And Stirling's approximation has the property that the ratio

$$\frac{n!}{\sqrt{2\pi n} \left(\frac{n}{e}\right)^n}$$

approaches 1 as  $n$  grows to infinity, *therefore a single solution can be selected from possibilities*

Applying Laplace's transform we have

$$\int_0^\infty e^{n(\ln y - y)} dy \sim \sqrt{\frac{2\pi}{n}} e^{-n}$$

which recovers the Stirling's formula, allowing observation of all energies in a visual circular

$$\lim_{n \rightarrow +\infty} \frac{\int_a^b e^{nf(x)} dx}{e^{nf(x_0)} \sqrt{\frac{2\pi}{n(-f''(x_0))}}} = 1$$

dial, with each representing a possible outcome

